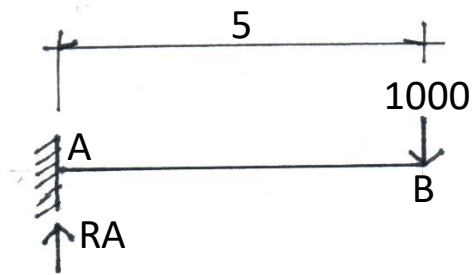


BAB 6 GARIS PENGARUH

6.1 Hitung momen dan gaya lintang dengan metode garis pengaruh, $P = 1000 \text{ kg}$



Cara biasa :

$$\Sigma V = 0 \rightarrow RA - P = 0 \rightarrow RA - 1000 = 0 \rightarrow RA = 1000 \text{ kg}$$

$$MA = P \cdot 5 = 1000 \cdot 5 = 5000 \text{ kgm}$$

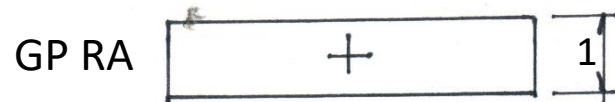
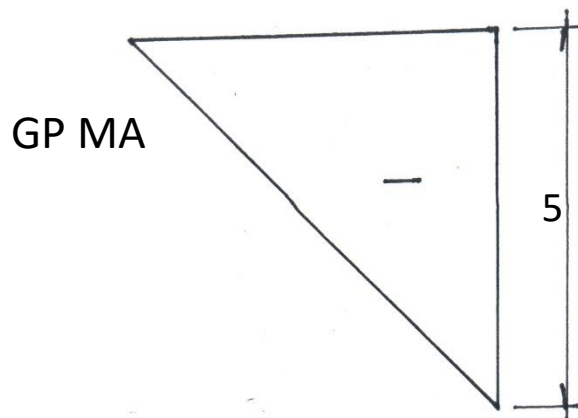
Cara garis pengaruh :

Momen : ordinat $Y = L = 5 \text{ m}$

$$MA = P \cdot Y = 1000 \cdot 5 = 5000 \text{ kgm}$$

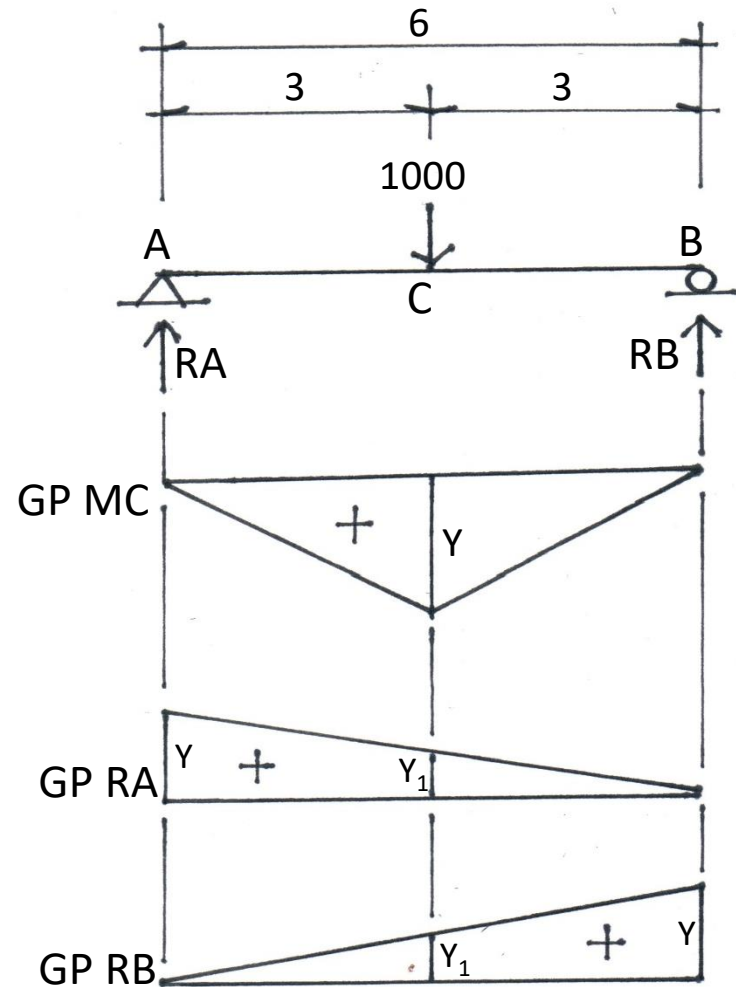
Gaya lintang : ordinat $Y = 1$

$$RA = P \cdot 1 = 1000 \cdot 1 = 1000 \text{ kg}$$



6.2 Hitung momen dan gaya lintang dengan metode garis pengaruh,

$$P = 1000 \text{ kg.}$$



Cara biasa : $\Sigma V = 0 \rightarrow RA + RB = P \rightarrow RA + RB = 1000$

$$RA = RB = 0,5 \cdot 1000 = \mathbf{500 \text{ kg}}$$

$$MC = 500 \cdot 3 = \mathbf{1500 \text{ kg}}$$

Garis pengaruh :

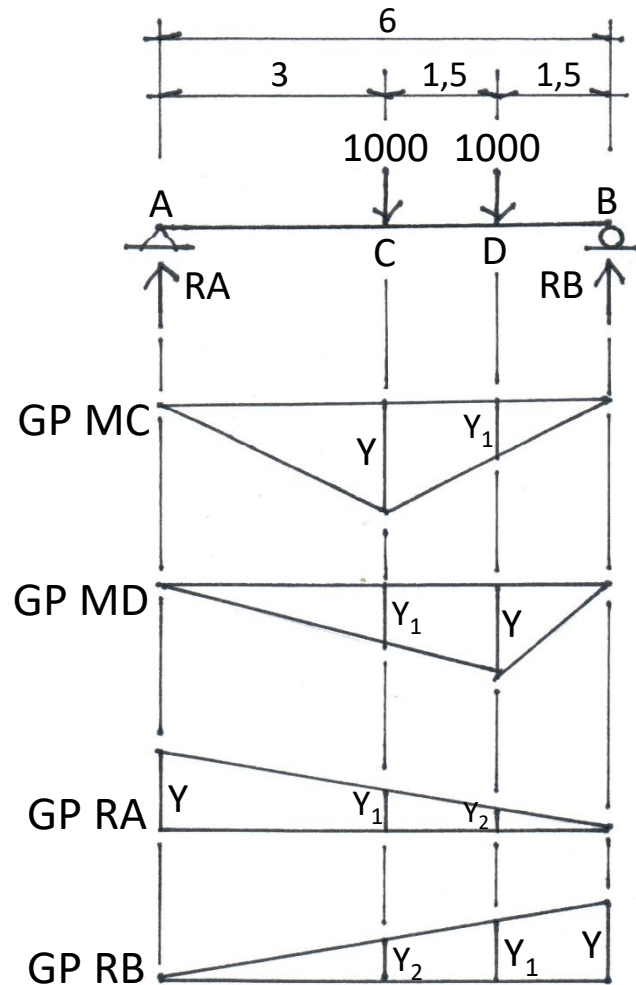
Momen \rightarrow ordinat : $Y = \frac{3 \cdot 3}{6} = 1,5 \rightarrow MC = 1000 \cdot 1,5 = \mathbf{1500 \text{ kgm}}$

Gaya lintang : RA \rightarrow ordinat : $Y = 1$; $\frac{Y_1}{1} = \frac{3}{6} \rightarrow Y_1 = 0,5$

$$RA = 1000 \cdot 0,5 = \mathbf{500 \text{ kg}}$$

$$RB = 1000 \cdot 0,5 = \mathbf{500 \text{ kg}}$$

6.3 Hitung momen dan gaya lintang dengan metode garis pengaruh, $P = 1000 \text{ kg}$



Cara biasa : $\Sigma M_B = 0 \rightarrow RA \cdot 6 - 1000 \cdot 1,5 - 1000 \cdot 3 = 0$

$6 RA - 1500 - 3000 = 0 \rightarrow 6 RA = 4500 \rightarrow \mathbf{RA = 750 \text{ kg}}$

$\Sigma M_A = 0 \rightarrow RB \cdot 6 - 1000 \cdot 3 - 1000 \cdot 4,5 = 0 \rightarrow 6 RB - 3000 - 4500 = 0$

$6 RB = 7500 \rightarrow \mathbf{RB = 1250 \text{ kg}}$

$MC = 750 \cdot 3 = \mathbf{2250 \text{ kgm}} ; MD = 1250 \cdot 1,5 = \mathbf{1875 \text{ kgm}}$

Garis pengaruh : MC \rightarrow ordinat : $Y = \frac{3 \cdot 3}{6} = 1,5 ; \frac{Y_1}{1,5} = \frac{1,5}{3} \rightarrow Y_1 = 0,75$

$MC = 1000 \cdot 1,5 + 1000 \cdot 0,75 = 1500 + 750 = \mathbf{2250 \text{ kgm}}$

MD \rightarrow ordinat : $Y = \frac{4,5 \cdot 1,5}{6} = 1,125 ; \frac{Y_1}{1,125} = \frac{3}{4,5} \rightarrow Y_1 = 0,75$

$MD = 1000 \cdot 0,75 + 1000 \cdot 1,125 = 750 + 1125 = \mathbf{1875 \text{ kgm}}$

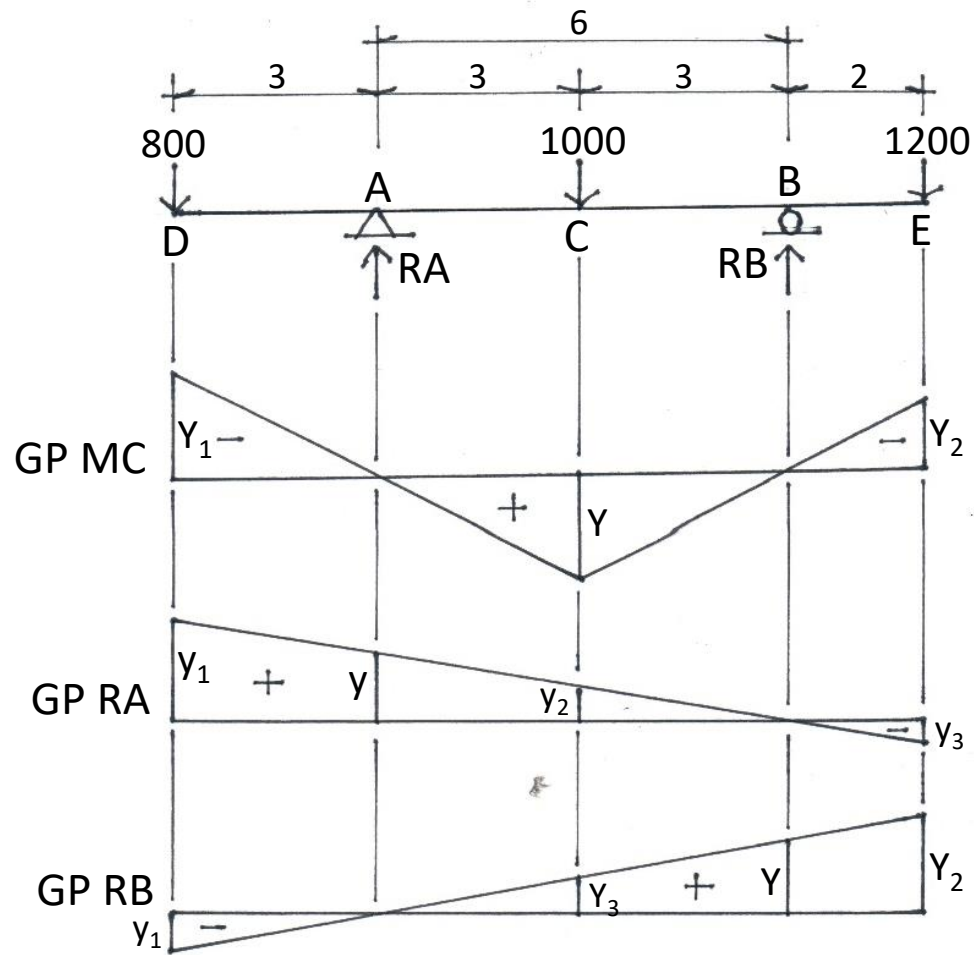
RA \rightarrow ordinat : $Y = 1 ; \frac{Y_1}{1} = \frac{3}{6} \rightarrow Y_1 = 0,5 ; \frac{Y_2}{1} = \frac{1,5}{6} \rightarrow Y_2 = 0,25$

$RA = 1000 \cdot 0,5 + 1000 \cdot 0,25 = 500 + 250 = \mathbf{750 \text{ kg}}$

RB \rightarrow ordinat : $Y = 1 ; \frac{Y_1}{1} = \frac{4,5}{6} \rightarrow Y_1 = 0,75 ; \frac{Y_2}{1} = \frac{3}{6} \rightarrow Y_2 = 0,5$

$RB = 1000 \cdot 0,5 + 1000 \cdot 0,75 = 500 + 750 = \mathbf{1250 \text{ kg}}$

6.4 Hitung momen dan gaya lintang dengan metode garis pengaruh, $P_1= 800 \text{ kg}$, $P_2= 1000 \text{ kg}$, $P_3= 1200 \text{ kg}$



Cara biasa : $\Sigma M_B = 0 \rightarrow R_A = \mathbf{1300 \text{ kg}}$

$\Sigma M_A = 0 \rightarrow R_B = \mathbf{1700 \text{ kg}}$

$\Sigma V = 0 \rightarrow 1300 + 1700 = 800 + 1000 + 1200$

$3000 = 3000 \rightarrow \text{ok}$

$M_A = 800 \cdot 3 = 2400 \text{ kgm}$; $M_B = 1200 \cdot 2 = \mathbf{2400 \text{ kgm}}$

$M_C = 1300 \cdot 3 - 800 \cdot 6 = 3900 - 4800 = \mathbf{-900 \text{ kgm}}$

Garis pengaruh :

Mom = en di C (MC) \rightarrow ordinat : $Y = \frac{3 \cdot 3}{6} = 1,5$

$\frac{1,5}{Y_1+1,5} = \frac{3}{6} \rightarrow Y_1 = 1,5$; $\frac{1,5}{Y_2+1,5} = \frac{3}{5} \rightarrow Y_2 = 1$

$M_C = 1000 \cdot 1,5 - 800 \cdot 1,5 - 1200 \cdot 1 = \mathbf{-900 \text{ kgm}}$

GP RA \rightarrow ordinat : $Y = 1$; $\frac{1}{Y_1} = \frac{6}{9} \rightarrow Y_1 = 1,5$

$\frac{Y_2}{1} = \frac{3}{6} \rightarrow Y_2 = 0,5$; $\frac{1}{Y_3+1} = \frac{6}{8} \rightarrow Y_3 = 0,333$

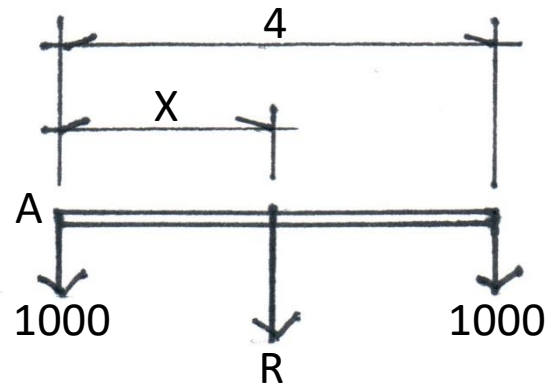
$R_A = 800 \cdot 1,5 + 1000 \cdot 0,5 - 1200 \cdot 0,333 = \mathbf{1300 \text{ kg}}$

GP RB \rightarrow ordinat : $Y = 1$; $\frac{1}{Y_2} = \frac{6}{8} \rightarrow Y_2 = 1,333$

$\frac{Y_3}{1} = \frac{3}{6} \rightarrow Y_3 = 0,5$; $\frac{1}{Y_1+1} = \frac{6}{9} \rightarrow Y_1 = 0,5$

$R_B = 1200 \cdot 1,333 + 1000 \cdot 0,5 - 800 \cdot 0,5 = \mathbf{1700 \text{ kg}}$

6.5 Hitung besaran R dan letaknya, P = 1000 kg

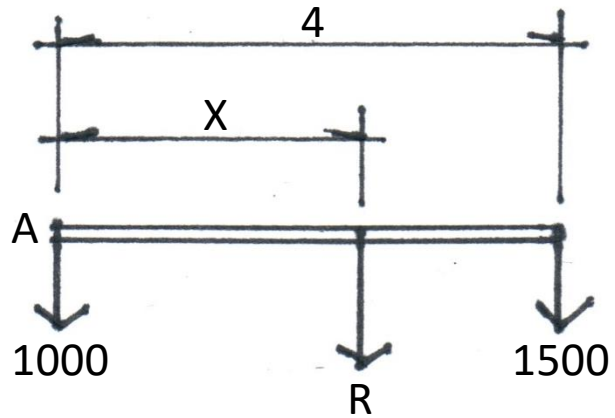


$$P = 1000 \text{ kg}$$

$$R = \Sigma P = 2 \cdot 1000 = \mathbf{2000 \text{ kg}}$$

$$R \cdot X = P \cdot 4 \rightarrow 2000 X = 1000 \cdot 4 \rightarrow 2000 X = 4000 \rightarrow \mathbf{X = 2 \text{ m dari A}}$$

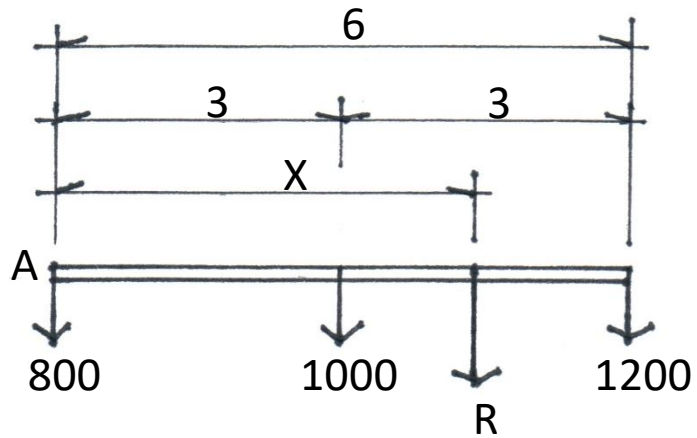
6.6 Hitung besaran R dan letaknya, $P_1 = 1000 \text{ kg}$; $P_2 = 1500 \text{ kg}$



$$R = \Sigma P = P_1 + P_2 = 1000 + 1500 = \mathbf{2500 \text{ kg}}$$

$$R \cdot X = P_2 \cdot 4 \rightarrow 2500 X = 1500 \cdot 4 \rightarrow 2500 X = 6000 \rightarrow \mathbf{X = 2,4 \text{ m dari A}}$$

6.7 Hitung besaran R dan letaknya, $P_1 = 800 \text{ kg}$; $P_2 = 1000 \text{ kg}$;
 $P_3 = 1200 \text{ kg}$

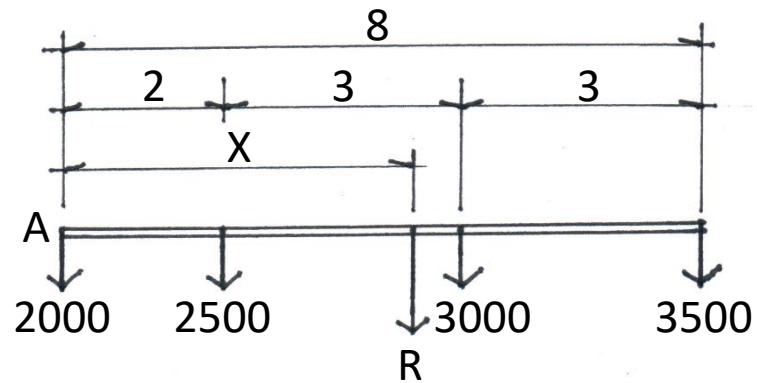


$$R = \Sigma P = P_1 + P_2 + P_3 = 800 + 1000 + 1200 = \mathbf{3000 \text{ kg}}$$

$$R \cdot X = P_2 \cdot 3 + P_3 \cdot 6 \rightarrow 3000 X = 1000 \cdot 3 + 1200 \cdot 6$$

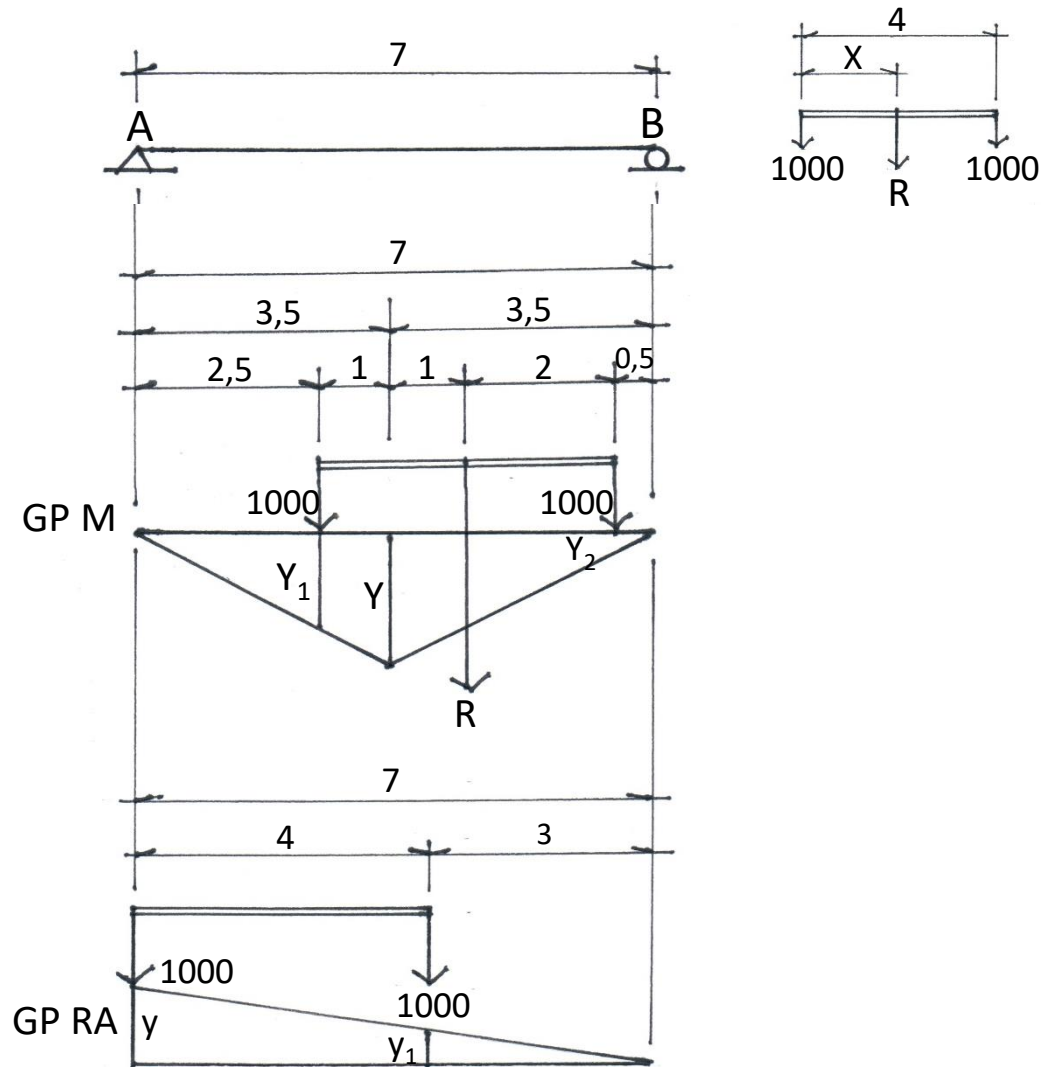
$$3000 X = 3000 + 7200 \rightarrow 3000 X = 10200 \rightarrow \mathbf{X = 3,4 \text{ m dari A}}$$

6.8 Hitung besaran R dan letaknya, $P_1 = 2000 \text{ kg}$; $P_2 = 2500 \text{ kg}$;
 $P_3 = 3000 \text{ kg}$; $P_4 = 3500 \text{ kg}$



$$R = \Sigma P = P_1 + P_2 + P_3 + P_4 = 2000 + 2500 + 3000 + 3500 = \mathbf{11000 \text{ kg}}$$
$$R \cdot X = P_2 \cdot 2 + P_3 \cdot 5 + P_4 \cdot 8 \rightarrow 11000 X = 2500 \cdot 2 + 3000 \cdot 5 + 3500 \cdot 8$$
$$11000 X = 5000 + 15000 + 28000$$
$$11000 X = 48000 \rightarrow \mathbf{X = 4,36 \text{ m dari A}}$$

6.9 Dengan metode garis pengaruh hitung momen maksimum dan gaya lintang maksimum.



$$R = 1000 + 1000 = \mathbf{2000 \text{ kg}}$$

$$2000 X = 1000 \cdot 4 \rightarrow 2000 X = 4000 \rightarrow \mathbf{X = 2 \text{ m}}$$

$$\text{Momen} \rightarrow \text{ordinat} : Y = \frac{3,5 \cdot 3,5}{7} = 1,75 \text{ m}$$

$$\frac{Y_1}{1,75} = \frac{2,5}{3,5} \rightarrow Y_1 = 1,25 \text{ m} ; \frac{Y_2}{1,75} = \frac{0,5}{3,5} \rightarrow Y_2 = 0,25 \text{ m}$$

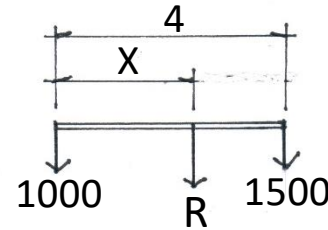
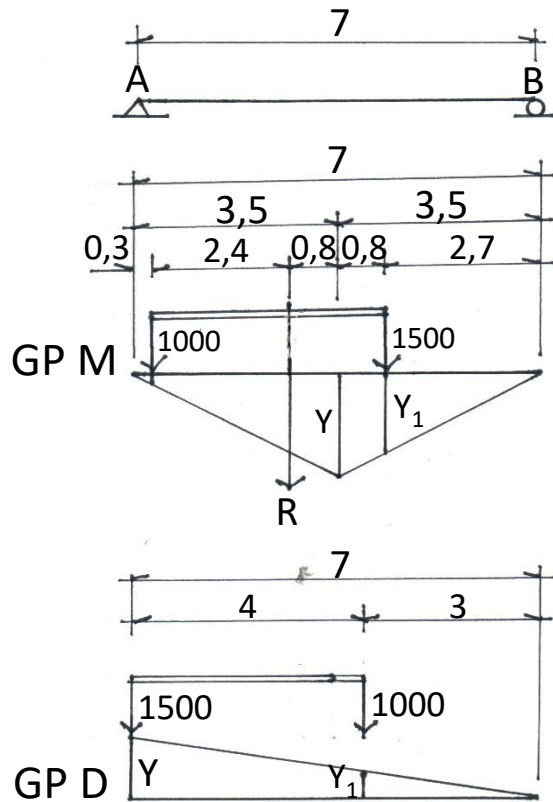
$$M \text{ maks} = 1000 \cdot 1,25 + 1000 \cdot 0,25 = 1250 + 250 = \mathbf{1500 \text{ kgm}}$$

$$\text{Gaya lintang} \rightarrow \text{ordinat} : Y = 1$$

$$Y_1 = \frac{3}{7} = 0,429$$

$$RA = 1000 \cdot 1 + 1000 \cdot 0,429 = 1000 + 429 = \mathbf{1429 \text{ kg}}$$

6.10 Dengan metode garis pengaruh hitung momen maksimum dan gaya lintang maksimum, $P_1 = 1000 \text{ kg}$; $P_2 = 1500 \text{ kg}$



$$R = 1000 + 1500 = \mathbf{2500 \text{ kg}}$$

$$2500 X = 1500 \cdot 4 \rightarrow 2500 X = 6000 \rightarrow \mathbf{X = 2,4 \text{ m}}$$

$$\text{Momen} \rightarrow \text{ordinat} : Y = \frac{3,5 \cdot 3,5}{7} = 1,75 \text{ m} ; \frac{Y_1}{1,75} = \frac{2,7}{3,5} \rightarrow Y_1 = 1,35 \text{ m}$$

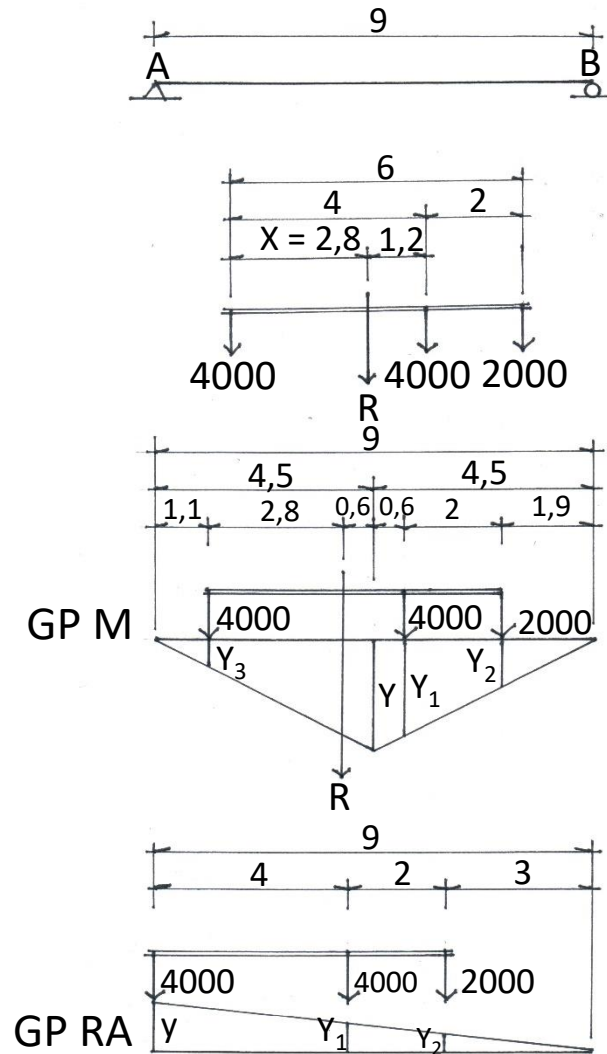
$$\frac{Y_2}{1,75} = \frac{2,7}{3,5} \rightarrow Y_2 = 0,15 \text{ m} ; M \text{ maks} = 1000 \cdot 0,15 + 1500 \cdot 1,35 = \mathbf{2175 \text{ kgm}}$$

$$\text{Gaya lintang (RA maks)} \rightarrow \text{ordinat} : Y = 1 ; \frac{Y_1}{1} = \frac{3}{7} \rightarrow Y_1 = 0,429$$

$$RA = 1500 \cdot 1 + 1000 \cdot 0,429 = 1500 + 429 = \mathbf{1929 \text{ kg}}$$

Catatan : untuk mendapatkan momen yang paling maksimum, Y di tengah-tengah antara R dan beban terdekat.

6.11 Dengan metode garis pengaruh hitung momen maksimum dan gaya lintang maksimum, $P_1 = 4000 \text{ kg}$; $P_2 = 4000 \text{ kg}$; $P_3 = 2000 \text{ kg}$



$$R = 4000 + 4000 + 4000 + 2000 = \mathbf{10000 \text{ kg}}$$

$$R \cdot X = 4000 \cdot 4 + 2000 \cdot 6 \rightarrow 10000 X = 16000 + 12000 \rightarrow$$

$$10000 X = 28000 \rightarrow \mathbf{X = 2,8 \text{ m}}$$

$$\text{Momen} \rightarrow \text{ordinat} : Y = \frac{4,5 \cdot 4,5}{9} = 2,25 \text{ m} ; \frac{Y_1}{2,25} = \frac{3,9}{4,5} \rightarrow Y_1 = 1,95 \text{ m}$$

$$\frac{Y_2}{2,25} = \frac{1,9}{4,5} \rightarrow Y_2 = 0,95 \text{ m} ; \frac{Y_3}{2,25} = \frac{1,1}{4,5} \rightarrow Y_3 = 0,55 \text{ m}$$

$$\begin{aligned} M \text{ maks} &= 4000 \cdot 0,55 + 4000 \cdot 1,95 + 2000 \cdot 0,95 \\ &= 2200 + 7800 + 1900 = \mathbf{11900 \text{ kgm}} \end{aligned}$$

$$\text{Gaya lintang} \rightarrow \text{ordinat} : Y = 1 ; \frac{Y_1}{1} = \frac{5}{9} \rightarrow Y_1 = 0,56 ; \frac{Y_2}{1} = \frac{3}{9} \rightarrow Y_2 = 0,33$$

$$R_A = 4000 \cdot 1 + 4000 \cdot 0,56 + 2000 \cdot 0,33 = 4000 + 2240 + 660 = \mathbf{6900 \text{ kg}}$$