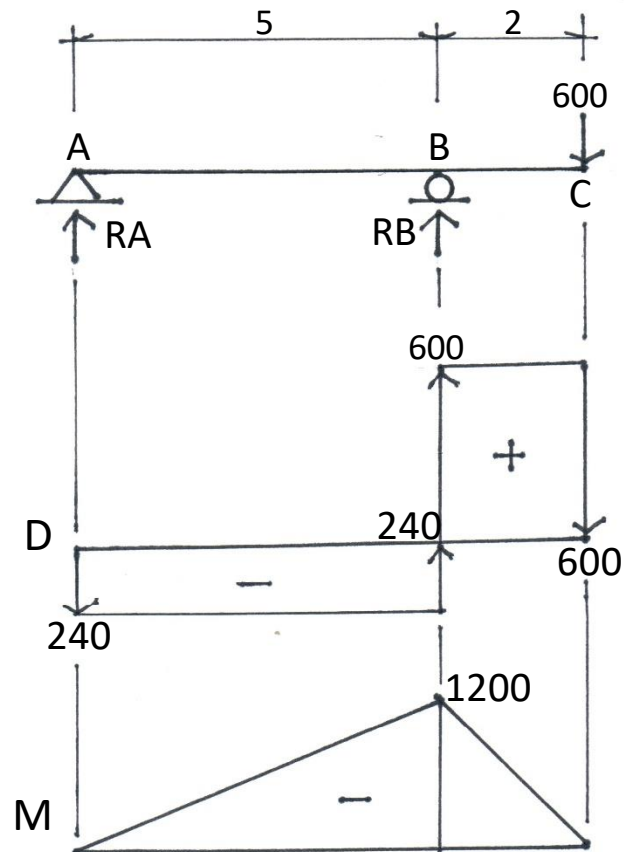


## BAB 4 BALOK SEDERHANA DENGAN TAMBAHAN KANTILEVEL

4.1 Gambar bidang : gaya lintang dan momen  $\rightarrow P = 600 \text{ kg}$



$$\Sigma M_B = 0 \rightarrow RA \cdot 5 + P \cdot 2 = 0 \rightarrow 5 RA + 600 \cdot 2 = 0 \rightarrow 5 RA = -1200$$

$$RA = -240 \text{ kg}$$

$$\Sigma M_A = 0 \rightarrow RB \cdot 5 - P \cdot 7 = 0 \rightarrow 5 RB - 600 \cdot 7 = 0 \rightarrow 5 RB = 4200$$

$$RB = 840 \text{ kg}$$

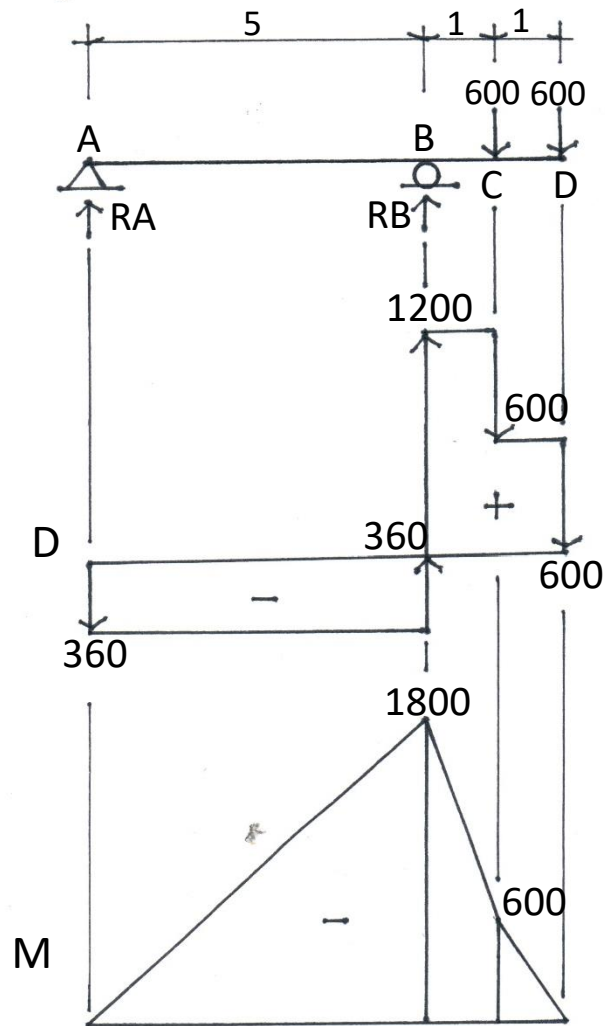
$$\Sigma V = 0 \rightarrow RA + RB = P \rightarrow -240 + 840 = 600 \rightarrow 600 = 600 \rightarrow \text{ok}$$

$$R_{BC} = P = 600 \text{ kg}$$

$$R_{BA} = RB - R_{BC} = 840 - 600 = 240 \text{ kg}$$

$$M_B = P \cdot 2 = 600 \cdot 2 = 1200 \text{ kgm}$$

## 4.2 Gambar bidang : gaya lintang dan momen $\rightarrow P = 600 \text{ kg}$



$$\begin{aligned} \sum M_B = 0 &\rightarrow R_A \cdot 5 + P \cdot 1 + P \cdot 2 = 0 \rightarrow 5 R_A + 600 \cdot 1 + 600 \cdot 2 = 0 \\ 5 R_A + 600 + 1200 &= 0 \rightarrow 5 R_A = -1800 \rightarrow \mathbf{R_A = -360 \text{ kg}} \end{aligned}$$

$$\begin{aligned} \sum M_B = 0 &\rightarrow R_B \cdot 5 - P \cdot 6 - P \cdot 7 = 0 \rightarrow 5 R_B - 600 \cdot 6 - 600 \cdot 7 = 0 \\ 5 R_B - 3600 - 4200 &= 0 \rightarrow 5 R_B = 7800 \rightarrow \mathbf{R_B = 1560 \text{ kg}} \end{aligned}$$

$$\begin{aligned} \sum V = 0 &\rightarrow R_A + R_B = 2 P \rightarrow -360 + 1560 = 2 \cdot 600 \\ 1200 &= 1200 \rightarrow \text{ok} \end{aligned}$$

$$R_{BD} = 2 P = 2 \cdot 600 = 1200 \text{ kg}$$

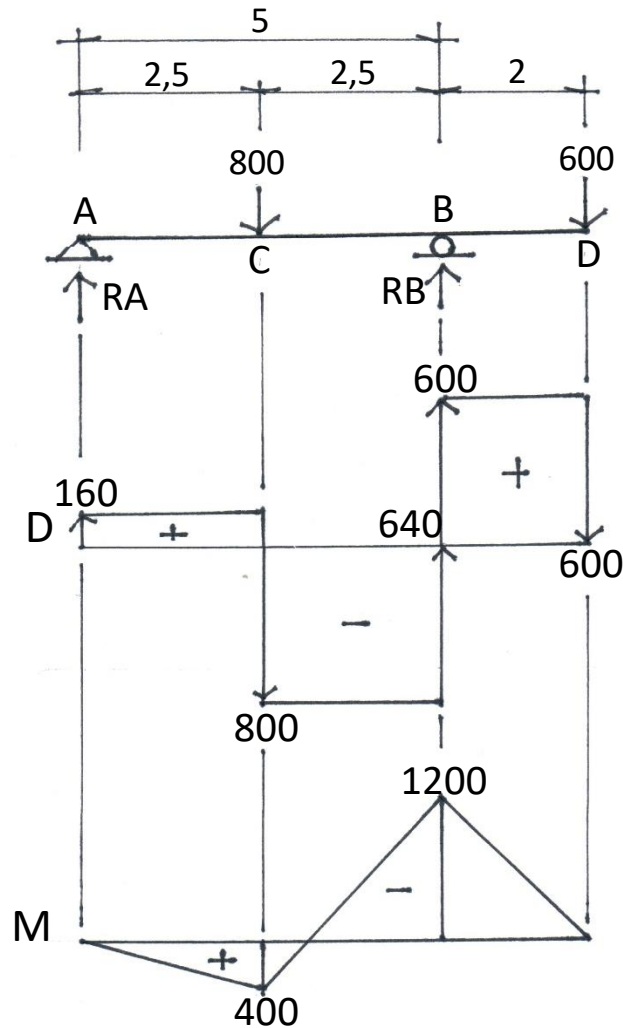
$$R_{BA} = R_B - R_{BD} = 1560 - 1200 = 360 \text{ kg}$$

$$M_B = P \cdot 1 + P \cdot 2 = 600 \cdot 1 + 600 \cdot 2 = 600 + 1200 = \mathbf{1800 \text{ kg}}$$

$$M_C = P \cdot 1 = 600 \cdot 1 = \mathbf{600 \text{ kgm}}$$

### 4.3 Gambar bidang : gaya lintang dan momen, $P_1 = 800 \text{ kg}$

$$P_2 = 600 \text{ kg}$$



$$\begin{aligned} \Sigma M_B = 0 &\rightarrow RA \cdot 5 + P_2 \cdot 2 - P_1 \cdot 2,5 = 0 \rightarrow 5 RA + 600 \cdot 2 - 800 \cdot 2,5 = 0 \\ 5 RA + 1200 - 2000 &= 0 \rightarrow 5 RA - 800 = 0 \rightarrow 5 RA = 800 \end{aligned}$$

$$RA = 160 \text{ kg}$$

$$\begin{aligned} \Sigma M_A = 0 &\rightarrow RB \cdot 5 - P_1 \cdot 2,5 - P_2 \cdot 7 = 0 \rightarrow 5 RB - 800 \cdot 2,5 - 600 \cdot 7 = 0 \\ 5 RB - 2000 - 4200 &= 0 \rightarrow 5 RB - 6200 = 0 \rightarrow 5 RB = 6200 \end{aligned}$$

$$RB = 1240 \text{ kg}$$

$$\begin{aligned} \Sigma V = 0 &\rightarrow RA + RB = P_1 + P_2 \rightarrow 160 + 1240 = 800 + 600 \\ 1400 &= 1400 \rightarrow \text{ok} \end{aligned}$$

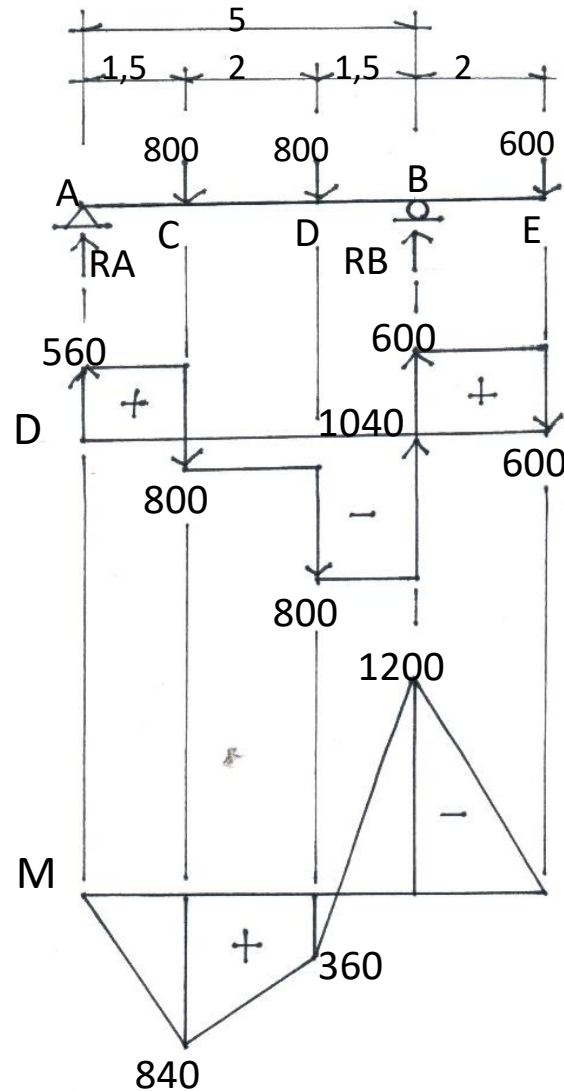
$$RBD = P_2 = 600 \text{ kg} ; RBA = RB - RBD = 1240 - 600 = 640 \text{ kg}$$

$$MB = P_2 \cdot 2 = 600 \cdot 2 = 1200 \text{ kgm}$$

$$MC = RA \cdot 2,5 = 160 \cdot 2,5 = 400 \text{ kgm}$$

#### 4.4 Gambar bidang : gaya lintang dan momen, $P_1 = 800 \text{ kg}$

$$P_2 = 600 \text{ kg}$$



$$\Sigma M_B = 0 \rightarrow RA \cdot 5 + P_2 \cdot 2 - P_1 \cdot 1,5 - P_1 \cdot 3,5 = 0$$

$$5 RA + 600 \cdot 2 - 800 \cdot 1,5 - 800 \cdot 3,5 = 0 \rightarrow 5 RA + 1200 - 1200 - 2800 = 0$$

$$5 RA - 2800 = 0 \rightarrow 5 RA = 2800 \rightarrow \mathbf{RA = 560 \text{ kg}}$$

$$\Sigma M_A = 0 \rightarrow RB \cdot 5 - P_1 \cdot 1,5 - P_1 \cdot 3,5 - P_2 \cdot 7 = 0$$

$$5 RB - 800 \cdot 1,5 - 800 \cdot 3,5 - 600 \cdot 7 = 0 \rightarrow 5 RB - 1200 - 2800 - 4200 = 0$$

$$5 RB - 8200 = 0 \rightarrow \mathbf{RB = 1640 \text{ kg}}$$

$$\Sigma V = 0 \rightarrow RA + RB = 2 P_1 + P_2 \rightarrow 560 + 1640 = 2 \cdot 800 + 600$$

$$2200 = 2200 \rightarrow \text{ok}$$

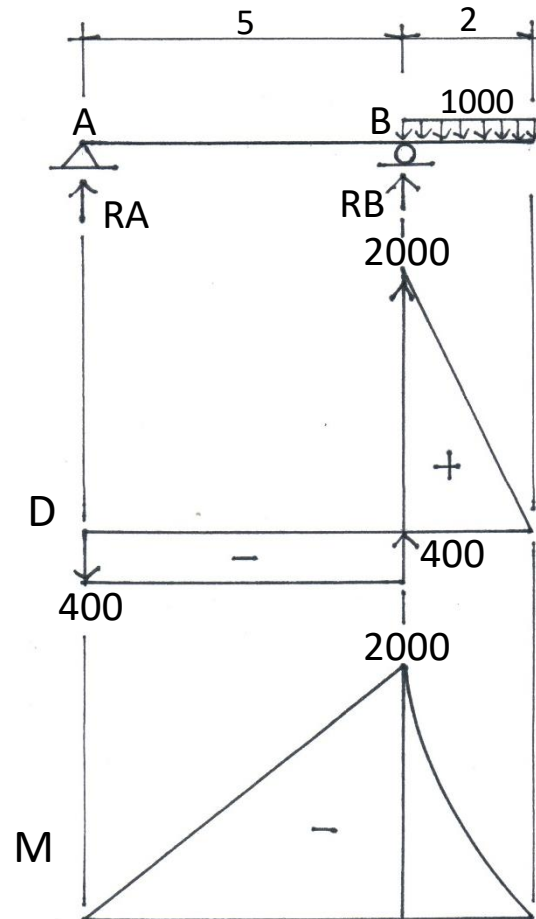
$$R_{BE} = P_2 = 600 \text{ kg} ; R_{BA} = RB - R_{BE} = 1640 - 600 = 1040 \text{ kg}$$

$$M_B = P_2 \cdot 2 = 600 \cdot 2 = \mathbf{1200 \text{ kgm}}$$

$$M_C = RA \cdot 1,5 = 560 \cdot 1,5 = \mathbf{840 \text{ kgm}}$$

$$M_D = RB \cdot 1,5 - P_2 \cdot 3,5 = 1640 \cdot 1,5 - 600 \cdot 3,5 = 2460 - 2100 = \mathbf{360 \text{ kgm}}$$

## 4.5 Gambar bidang : gaya lintang dan momen, $W = 1000 \text{ kg/m}$



$$\Sigma M_B = 0 \rightarrow RA \cdot 5 + W \cdot 2 \cdot 1 = 0 \rightarrow 5 RA + 1000 \cdot 2 = 0 \rightarrow 5 RA = -2000$$

$$RA = -400 \text{ kg}$$

$$\Sigma M_A = 0 \rightarrow RB \cdot 5 - W \cdot 2 \cdot 6 = 0 \rightarrow 5 RB - 1000 \cdot 12 = 0 \rightarrow 5 RB = 12000$$

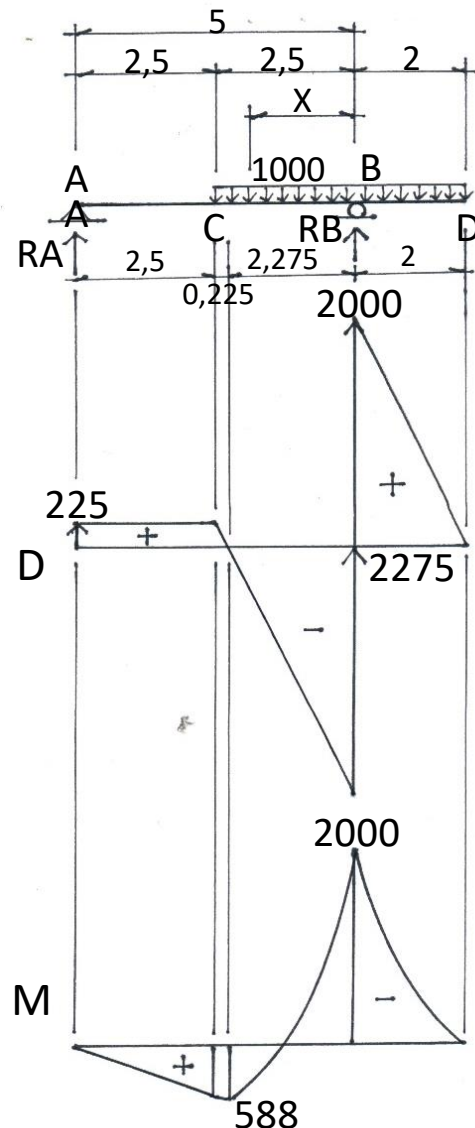
$$RB = 2400 \text{ kg}$$

$$\Sigma V = 0 \rightarrow RA + RB = Q \rightarrow -400 + 2400 = 1000 \cdot 2$$

$$2000 = 2000 \rightarrow \text{ok}$$

$$MB = W \cdot 2 \cdot 1 = 1000 \cdot 2 = 2000 \text{ kgm}$$

## 4.6 Gambar bidang : gaya lintang dan momen, $W = 1000 \text{ kg/m}$



$$\begin{aligned} \sum M_B = 0 &\rightarrow R_A \cdot 5 + W \cdot 2 \cdot 1 - W \cdot 2,5 \cdot 1,25 = 0 \rightarrow 5 R_A + 1000 \cdot 2 - 1000 \cdot 3,125 = 0 \\ 5 R_A + 2000 - 3125 &= 0 \rightarrow 5 R_A - 1125 = 0 \rightarrow 5 R_A = 1125 \rightarrow \mathbf{R_A = 225 \text{ kg}} \end{aligned}$$

$$\begin{aligned} \sum M_A = 0 &\rightarrow 5 R_B - W \cdot 2,5 \cdot 3,75 - W \cdot 2 \cdot 6 = 0 \rightarrow 5 R_B - 1000 \cdot 9,375 - 1000 \cdot 12 = 0 \\ 5 R_B - 9375 - 12000 &= 0 \rightarrow 5 R_B - 21375 = 0 \rightarrow 5 R_B = 21375 \rightarrow \mathbf{R_B = 4275 \text{ kg}} \end{aligned}$$

$$\sum V = 0 \rightarrow R_A + R_B = Q \rightarrow 225 + 4275 = 1000 \cdot 4,5 \rightarrow 4500 = 4500 \rightarrow \text{ok}$$

$$R_{BD} = Q = 1000 \cdot 2 = 2000 \text{ kg}$$

$$R_{BA} = R_B - R_{BD} = 4275 - 2000 = 2275 \text{ kg}$$

$$\begin{aligned} M_X &= R_B \cdot X - W \cdot 2 (1 + X) - W X \cdot 0,5 X = 4275 X - 1000 \cdot 2 (1 + X) - 1000 \cdot 0,5 X^2 \\ &= 4275 X - 2000 - 2000 X - 500 X^2 = 2275 X - 2000 - 500 X^2 \end{aligned}$$

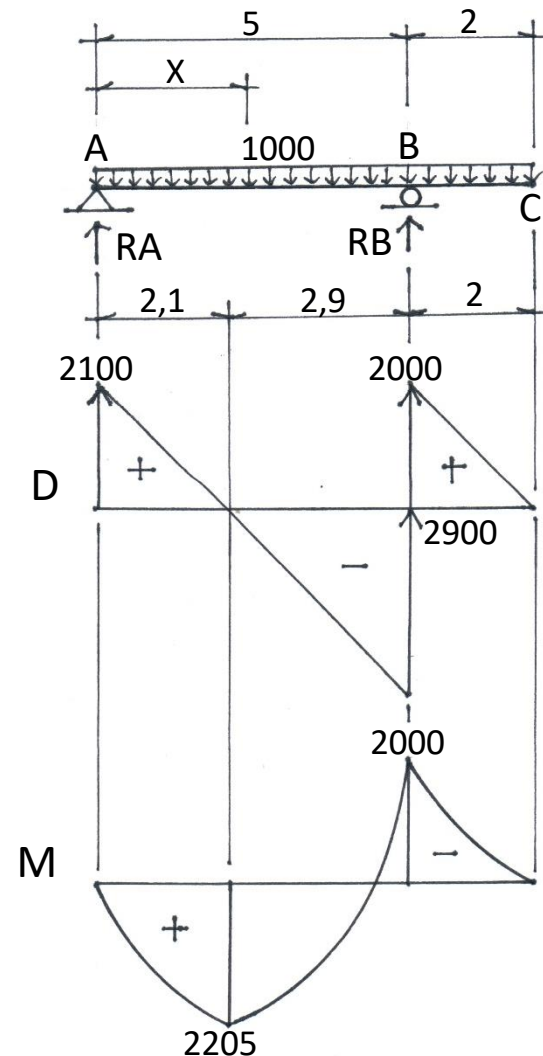
$$dM_X/dX = 2275 - 1000 X \rightarrow dM_X/dX = 0 \rightarrow 1000 X = 2275 \rightarrow X = 2,275 \text{ m}$$

$$M_{\text{maks}} = 2275 \cdot 2,275 - 2000 - 500 \cdot 2,275^2 = 5176 - 2000 - 2588 = \mathbf{588 \text{ kgm}}$$

$$M_B = W \cdot 2 \cdot 1 = 1000 \cdot 2 = \mathbf{2000 \text{ kgm}}$$

$$M_C = R_A \cdot 2,5 = 225 \cdot 2,5 = \mathbf{653 \text{ kgm}}$$

## 4.7 Gambar bidang : gaya lintang dan momen, $W = 1000 \text{ kg/m}$



$$\Sigma M_B = 0 \rightarrow R_A \cdot 5 + W \cdot 2 \cdot 1 - W \cdot 5 \cdot 2,5 = 0 \rightarrow 5 R_A + 1000 \cdot 2 - 1000 \cdot 12,5 = 0$$

$$5 R_A + 2000 - 12500 = 0 \rightarrow 5 R_A - 10500 = 0 \rightarrow 5 R_A = 10500$$

$$\mathbf{R_A = 2100 \text{ kg}}$$

$$\Sigma M_A = 0 \rightarrow R_B \cdot 5 - W \cdot 5 \cdot 2,5 - W \cdot 2 \cdot 6 = 0 \rightarrow 5 R_B - 1000 \cdot 12,5 - 1000 \cdot 12 = 0$$

$$5 R_B - 12500 - 12000 = 0 \rightarrow 5 R_B - 24500 = 0 \rightarrow 5 R_B = 24500$$

$$\mathbf{R_B = 4900 \text{ kg}}$$

$$\Sigma V = 0 \rightarrow R_A + R_B = Q \rightarrow 2100 + 4900 = 1000 \cdot 7$$

$$7000 = 7000 \rightarrow \text{ok}$$

$$R_{BC} = Q = 1000 \cdot 2 = 2000 \text{ kg}$$

$$R_{BA} = R_B - R_{BC} = 4900 - 2000 = 2900 \text{ kg}$$

$$M_X = R_A \cdot X - 0,5 W X^2 = 2100 X - 0,5 \cdot 1000 X^2$$

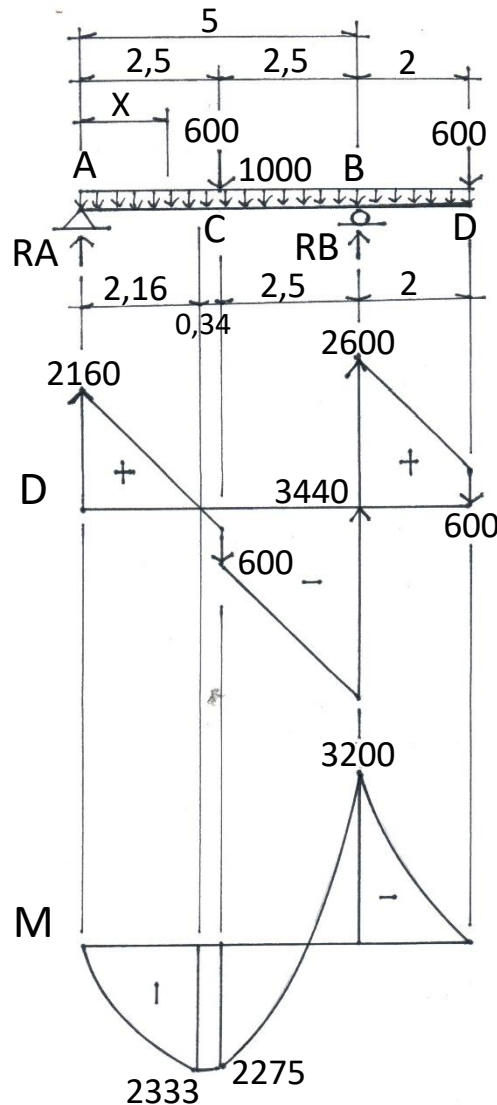
$$dM_X / dX = 2100 - 1000 X \rightarrow dM_X / dX = 0 \rightarrow 1000 X = 2100 \rightarrow X = 2,1 \text{ m}$$

$$M_{\text{maks}} = 2100 \cdot 2,1 - 500 \cdot 2,1^2 = 4410 - 2205 = \mathbf{2205 \text{ kgm}}$$

$$M_B = W \cdot 2 \cdot 1 = 1000 \cdot 2 = \mathbf{2000 \text{ kgm}}$$

## 4.8 Gambar bidang : gaya lintang dan momen, $W = 1000 \text{ kg/m}$

$$P = 600 \text{ kg}$$



$$\sum M_B = 0 \rightarrow R_A \cdot 5 + W \cdot 2 \cdot 1 - W \cdot 5 \cdot 2,5 + P \cdot 2 - P \cdot 2,5 = 0$$

$$5 R_A + 1000 \cdot 2 - 1000 \cdot 12,5 + 600 \cdot 2 - 600 \cdot 2,5 = 0$$

$$5 R_A + 2000 - 12500 + 1200 - 1500 = 0 \rightarrow 5 R_A - 10800 = 0$$

$$5 R_A = 10800 \rightarrow R_A = \mathbf{2160 \text{ kg}}$$

$$\sum M_A = 0 \rightarrow R_B \cdot 5 - W \cdot 7 \cdot 3,5 - P \cdot 2,5 - P \cdot 7 = 0$$

$$5 R_B - 1000 \cdot 24,5 - 600 \cdot 2,5 - 600 \cdot 7 = 0$$

$$5 R_B - 24500 - 1500 - 4200 = 0 \rightarrow 5 R_B - 30200 = 0$$

$$5 R_B = 30200 \rightarrow R_B = \mathbf{6040 \text{ kg}}$$

$$\sum V = 0 \rightarrow R_A + R_B = Q + 2 P \rightarrow 2160 + 6040 = 1000 \cdot 7 + 2 \cdot 600$$

$$8200 = 8200 \rightarrow \text{ok}$$

$$R_{BD} = 600 + 1000 \cdot 2 = 2600 \text{ kg}; R_{BA} = 6040 - 2600 = 3440 \text{ kg}$$

$$M_X = R_A \cdot X - 0,5 W X^2 = 2160 X - 0,5 \cdot 1000 X^2 \rightarrow dM_X/dX = 2160 - 1000 X$$

$$dM_X/dX = 0 \rightarrow 1000 X = 2160 \rightarrow X = 2,16 \text{ m}$$

$$M_{\text{maks}} = 2160 \cdot 2,16 - 500 \cdot 2,16^2 = 4666 - 2333 = \mathbf{2333 \text{ kgm}}$$

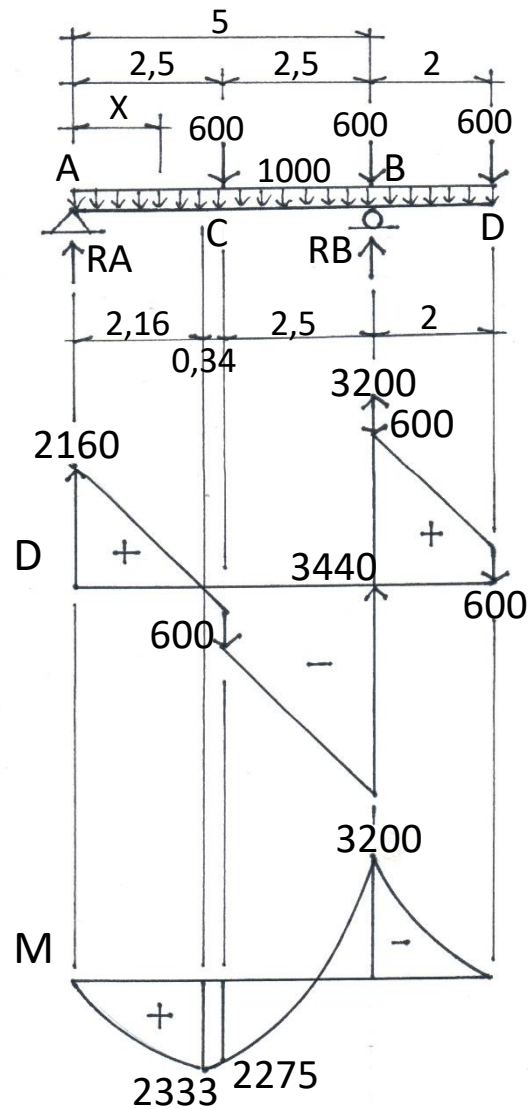
$$M_B = 600 \cdot 2 + 1000 \cdot 2 \cdot 1 = 1200 + 2000 = \mathbf{3200 \text{ kgm}}$$

$$M_C = 2160 \cdot 2,5 - 1000 \cdot 2,5 \cdot 1,25 = 5400 - 3125 = \mathbf{2275 \text{ kgm}}$$



## 4.9 Gambar bidang : gaya lintang dan momen, $W = 1000 \text{ kg/m}$

$$P = 600 \text{ kg}$$



$$\begin{aligned} \Sigma M_B = 0 &\rightarrow RA \cdot 5 + 600 \cdot 2 - 600 \cdot 2,5 + 1000 \cdot 2 \cdot 1 - 1000 \cdot 5 \cdot 2,5 = 0 \\ 5 RA + 1200 - 1500 + 2000 - 12500 &= 0 \rightarrow 5 RA - 10800 = 0 \\ 5 RA = 10800 &\rightarrow \mathbf{RA = 2160 \text{ kg}} \end{aligned}$$

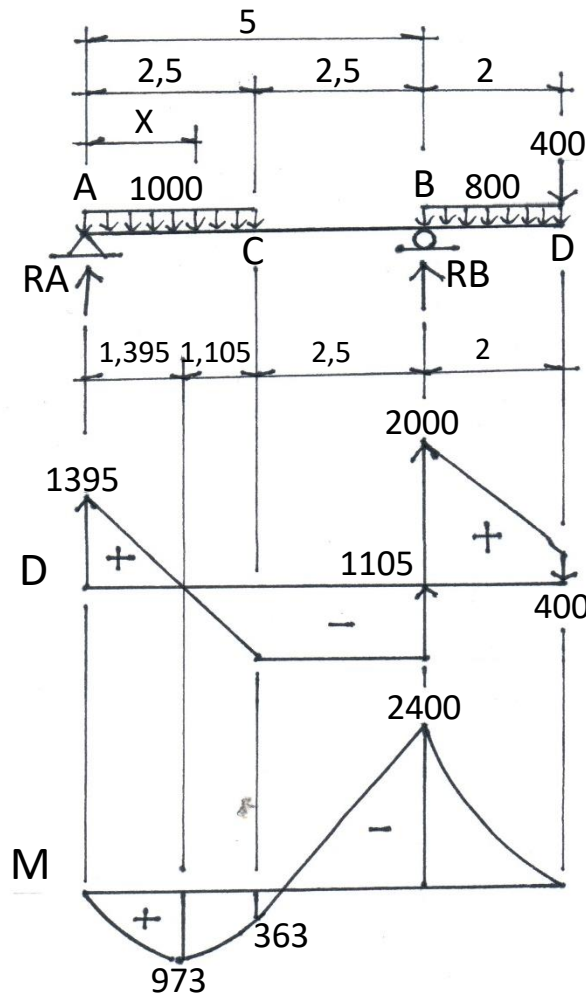
$$\begin{aligned} \Sigma M_A = 0 &\rightarrow RB \cdot 5 - 600 \cdot 2,5 - 600 \cdot 5 - 600 \cdot 7 - 1000 \cdot 7 \cdot 3,5 = 0 \\ 5 RB - 1500 - 3000 - 4200 - 24500 &= 0 \rightarrow 5 RB - 33200 = 0 \\ 5 RB = 33200 &\rightarrow \mathbf{RB = 6640 \text{ kg}} \end{aligned}$$

$$\begin{aligned} \Sigma V = 0 &\rightarrow 2160 + 6640 = 3 \cdot 600 + 1000 \cdot 7 \rightarrow 8800 = 8800 \rightarrow \text{ok} \\ R_{BD} &= 2 \cdot 1000 + 600 + 600 = 3200 \text{ kg} \\ R_{BA} &= 6640 - 3200 = 3440 \text{ kg} \end{aligned}$$

$$\begin{aligned} M_X &= 2160 X - 0,5 \cdot 1000 X^2 \rightarrow dM_X/dX = 2160 - 1000 X \\ dM_X/dX = 0 &\rightarrow 1000 X = 2160 \rightarrow X = 2,16 \text{ m} \\ M_{\text{maks}} &= 2160 \cdot 2,16 - 500 \cdot 2,16^2 = 4666 - 2333 = \mathbf{2333 \text{ kgm}} \\ M_B &= 600 \cdot 2 + 1000 \cdot 2 \cdot 1 = 1200 + 2000 = \mathbf{3200 \text{ kgm}} \\ M_C &= 2160 \cdot 2,5 - 1000 \cdot 2,5 \cdot 1,25 = 5400 - 3125 = \mathbf{2275 \text{ kgm}} \end{aligned}$$

4.10 Gambar bidang : gaya lintang dan momen,  $W_1 = 1000 \text{ kg/m}$ ,

$W_2 = 800 \text{ kg/m}$ ,  $P = 400 \text{ kg}$



$$\sum M_B = 0 \rightarrow R_A \cdot 5 + P \cdot 2 + W_2 \cdot 2 \cdot 1 - W_1 \cdot 2,5 \cdot 3,75 = 0$$

$$5 R_A + 400 \cdot 2 + 800 \cdot 2 - 1000 \cdot 9,375 = 0 \rightarrow 5 R_A + 800 + 1600 - 9375 = 0$$

$$5 R_A - 6975 = 0 \rightarrow 5 R_A = 6975 \rightarrow \mathbf{R_A = 1395 \text{ kg}}$$

$$\sum M_A = 0 \rightarrow R_B \cdot 5 - W_1 \cdot 2,5 \cdot 1,25 - W_2 \cdot 2 \cdot 6 - P \cdot 7 = 0$$

$$5 R_B - 1000 \cdot 3,125 - 800 \cdot 12 - 400 \cdot 7 = 0 \rightarrow 5 R_B - 3125 - 9600 - 2800 = 0$$

$$5 R_B - 15525 = 0 \rightarrow 5 R_B = 15525 \rightarrow \mathbf{R_B = 3105 \text{ kg}}$$

$$\sum V = 0 \rightarrow R_A + R_B = Q_1 + Q_2 + P \rightarrow 1395 + 3105 = 2500 + 1600 + 400$$

$$4500 = 4500 \rightarrow \text{ok}$$

$$R_{BD} = 400 + 800 \cdot 2 = 2000 \text{ kg}$$

$$R_{BA} = 3105 - 2000 = 1105 \text{ kg}$$

$$M_X = 1395 X - 0,5 \cdot 1000 X^2 \rightarrow dM_X/dX = 1395 - 1000 X$$

$$dM_X/dX = 0 \rightarrow 1000 X = 1395 \rightarrow X = 1,395 \text{ m}$$

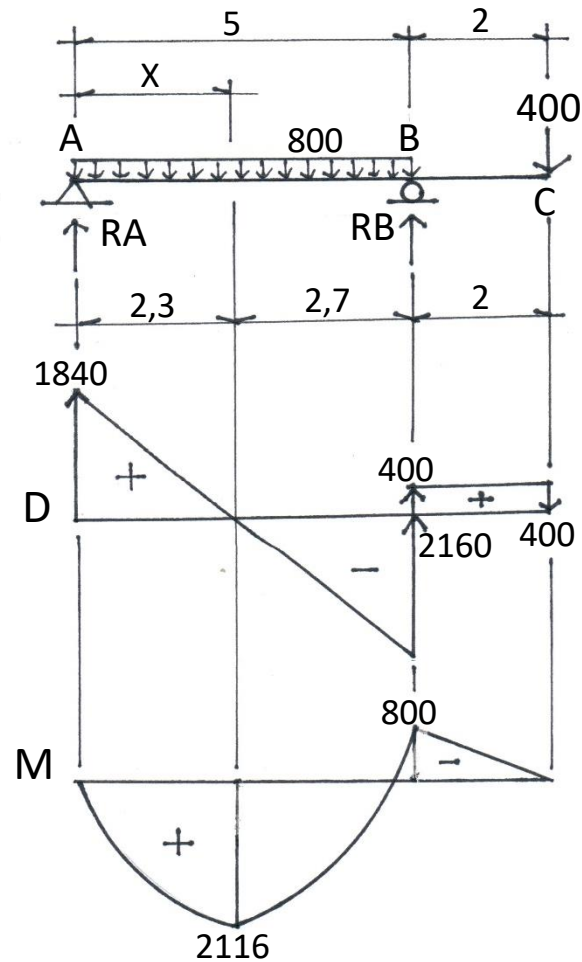
$$M_{\text{maks}} = 1395 \cdot 1,395 - 500 \cdot 1,395^2 = 1946 - 973 = \mathbf{973 \text{ kgm}}$$

$$M_B = 400 \cdot 2 + 800 \cdot 2 \cdot 1 = 800 + 1600 = \mathbf{2400 \text{ kgm}}$$

$$M_C = 1395 \cdot 2,5 - 1000 \cdot 2,5 \cdot 1,25 = 3488 - 3125 = \mathbf{363 \text{ kgm}}$$

## 4.11 Gambar bidang : gaya lintang dan momen, $W = 800 \text{ kg/m}$

$$P = 400 \text{ kg}$$



$$\begin{aligned} \Sigma M_B = 0 &\rightarrow RA \cdot 5 + 400 \cdot 2 - 800 \cdot 5 \cdot 2,5 = 0 \rightarrow 5 RA + 800 - 10000 = 0 \\ 5 RA - 9200 &= 0 \rightarrow 5 RA = 9200 \rightarrow \mathbf{RA = 1840 \text{ kg}} \end{aligned}$$

$$\begin{aligned} \Sigma M_A = 0 &\rightarrow RB \cdot 5 - 800 \cdot 5 \cdot 2,5 - 400 \cdot 7 = 0 \rightarrow 5 RB - 10000 - 2800 = 0 \\ 5 RB - 12800 &= 0 \rightarrow 5 RB = 12800 \rightarrow \mathbf{RB = 2560 \text{ kg}} \end{aligned}$$

$$\Sigma V = 0 \rightarrow 1840 + 2560 = 800 \cdot 5 + 400 \rightarrow 4400 = 4400 \rightarrow \text{ok}$$

$$\begin{aligned} MX &= 1840 X - 0,5 \cdot 800 X^2 \rightarrow dMX/dX = 1840 - 800 X \rightarrow dMX/dX = 0 \\ 800 X &= 1840 \rightarrow X = 2,3 \text{ m} \end{aligned}$$

$$M \text{ maks} = 1840 \cdot 2,3 - 400 \cdot 2,3^2 = 4232 - 2116 = \mathbf{2116 \text{ kgm}}$$

$$MB = 400 \cdot 2 = \mathbf{800 \text{ kgm}}$$